

Sydney Girls High School 2012 Trial Higher School Certificate Examination

Mathematics Extension 1

General Instructions

- Reading Time 5 minutes
- Working time 2 hours
- Write using black or blue pen Black pen is preferred
- Board-approved calculators may be used
- A table of standard integrals is provided at the back of this paper
- Show all necessary working in Ouestions 11 14

This is a trial paper ONLY. It does not necessarily reflect the format or the contents of the 2012 HSC Examination Paper in this subject.

Total marks -70

SECTION 1 – Pages 2 - 5

10 marks

- Attempt questions 1 10
- Allow about 15 minutes for this section

SECTION II – Pages 6 - 9

60 marks

- Attempt questions 11 14
- Allow about 1 hours 45 minutes for this section

Name: ______
Teacher:

Section I - Total Marks 10

Attempt Questions 1 – 10

Allow about 15 minutes for this section.

(1) Find
$$\lim_{x\to 0} \frac{\sin 3x}{4x}$$

- (a) $\frac{4}{3}$
- (b) 1
- (c) $\frac{3}{4}$
- (d) 0

(2)
$$\frac{d}{dx} \left[\sin(\log x) \right] =$$

- (a) $\cos(\log x)$
- (b) $\frac{\cos(\log x)}{x}$
- (c) $\frac{\sin(\log x)}{x}$
- (d) $-\cos(\log x)$
- (3) We can express $\sin x$ and $\cos x$ in terms of $\tan \frac{x}{2}$, for all values of x except
 - (a) $x = 2\pi, 6\pi, 8\pi, ...$
 - (b) $x = \pi, 3\pi, 5\pi, ...$
 - (c) $x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots$
 - (d) $x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \dots$

(4) Which of the following is an expression for $\int \cos^2 8x dx$

(a)
$$\frac{x}{2} - \frac{\sin 8x}{32} + c$$

(b)
$$\frac{x}{2} + \frac{\sin 8x}{32} + c$$

(c)
$$\frac{x}{2} - \frac{\sin 16x}{32} + c$$

(d)
$$\frac{x}{2} + \frac{\sin 16x}{32} + c$$

(5) Which of the following is the correct expression for $\int \frac{dx}{\sqrt{36-4x^2}}$

(a)
$$\frac{1}{2}\sin^{-1}\frac{x}{6}$$

(b)
$$\frac{1}{2}\sin^{-1}\frac{x}{3}$$

(c)
$$\frac{1}{4}\sin^{-1}\frac{x}{6}$$

(d)
$$\frac{1}{6}\sin^{-1}\frac{x}{3}$$

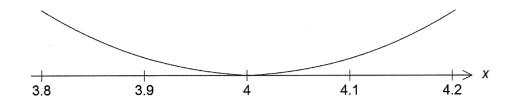
(6) The velocity, v metres per second, of a particle moving in a simple harmonic motion along the x-axis is given by the equation $v^2 = 64 - 16x^2$ What is the period, in seconds of the motion of the particle?

(a)
$$\frac{\pi}{8}$$

(b)
$$\frac{\pi}{4}$$

(c)
$$\frac{\pi}{2}$$

(7) Part of the graph of y = P(x), where P(x) is a polynomial of degree three, is shown below.



Which of the following could be the polynomial P(x)?

- (a) $(x-4)^3$
- (b) $(x-5)(x+4)^2$
- (c) $(x-1)(x-4)^2$
- (d) (x-1)(x+2)(x-4)
- (8) The radius of a sphere is increasing at a rate of 5 centimetres per minute.

What is the rate of increase of the surface area of the sphere, in cubic centimetres per minute, when the radius is 4 centimetres?

- (a) 32π
- (b) 64π
- (c) 100π
- (d) 160π
- (9) Which of the following represents the inverse function of $f(x) = \frac{5}{2x-6} 2$

(a)
$$f^{-1}(x) = \frac{5}{2x+4} + 3$$

(b)
$$f^{-1}(x) = \frac{5}{2x+4} - 3$$

(c)
$$f^{-1}(x) = 3 - \frac{5}{2x+4}$$

(d)
$$f^{-1}(x) = \frac{5}{x+2} + 6$$

(10)	How many solutions does the equation $\sin 2\theta = \cos \theta$ have in the domain
	$0 \le \theta \le 2\pi$?
	(a) 4

- (b) 3
- (c) 2
- (d) 1

END OF SECTION I

Section II - Total Marks 60

Attempt Questions 11 - 14Allow about 1 hour 45 minutes for this section

Answer all questions, starting each question on a new sheet of paper

Question 11 (15 marks)

2

(a) Find the acute angle between the lines (to the nearest degree) 3x+2y-6=0 and 2x-y+8=0

(b) A curve has parametric equations $x = \frac{t}{3}$, $y = 2t^2$. Find the Cartesian equation of this curve.

2

(c) Find $\int 2x\sqrt{x-5} dx$ using the substitution u = x-5

3

(d) If α , β and γ are the roots of the polynomial $5x^3 - 2x - 4 = 0$, find the value of $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$.

2

(e) Find the exact value of $\tan^{-1}(-\sqrt{3})$.

- 1
- (f) Find the coordinates of the point P that divides the interval AB externally in the ratio 3:2, where the coordinates of A and B are respectively $\left(-2,4\right)$ and $\left(3,-6\right)$.
- 2

(g) Solve $\frac{x}{2-x} \ge 2$.

3

Question 12 (15 marks) - Start a new page

Marks

(a) Prove by induction, that $5^n > 20n-1$ for $n \ge 1$, where n is an integer.

3

- (b) The probability that it rains on any particular day in London is $\frac{2}{3}$.
 - (i) What is the probability that it does not rain for a whole week in London?

2

(ii) What is the probability that it will rain on only two days during a whole week in London and that these two days are consecutive?

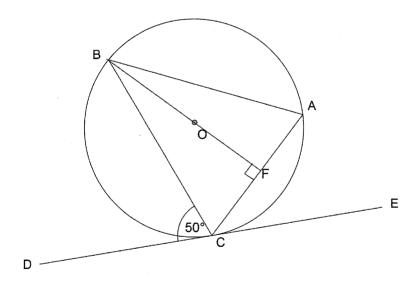
2

(c) Evaluate $\int_{0}^{\frac{\pi}{2}} \cos x \sin^2 x \ dx$

2

(d) The line DE is tangent to the circle at C. If $DCB = 50^{\circ}$, find the size of ACE giving full reasons.

2



2

(e) Sketch the graph of $y = sin^{-1} (x - 2)$

2

(f) The function $f(x) = \sin x - \frac{x}{2}$ has a zero near x = 2Taking x = 2 as a first approximation, use one application of Newton's method to find a second approximation to the zero. Give your answer correct to two decimal places.

Question 13 (15 marks) Start a new page

Marks

(a) Find the exact value of $\int_{0}^{2} \frac{dx}{4x^2 + 20}$

2

(b) An iron is cooling in a room of constant temperature 20^{0} C. At time t minutes its temperature T decreases according to the equation $\frac{dT}{dt} = -k(T-20)$ where k is a positive constant.

The initial temperature of the iron is 100^{0} C and it cools to 70^{0} C after 15 minutes.

(i) Verify that $T = 20 + Ae^{-kt}$ is a solution of this equation, where A is a constant.

1

(ii) Find the values of A and k.

2

2

(iii) How long will it take for the temperature of the iron to cool to to 25°C?

(c) Calculate the exact volume generated by the solid formed when $y = cos^{-1}x$ is rotated about the *y-axis* between y = 0 and $y = \pi$.

3

(d)
$$P(x) = x^4 + 5x^3 + 4x^2 - 8x - 8$$

i. Show that (x + 1)(x + 2) is a factor of P(x)

1

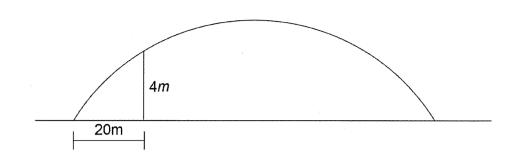
1

ii. Find Q(x) if P(x) = (x + 1)(x+2)Q(x)

(e) Solve the equation $\tan \theta = \sin 2\theta, 0 \le \theta \le 2\pi$

3

(a)



A projectile is fired with initial velocity Vms⁻¹ at an angle of θ from a point O on horizontal ground. After 5 seconds it just passes over a 4m high wall that is 20 metres from the point of projection. Assume the acceleration due to gravity is 10m^2 Assume the equations of displacement are $x = \text{Vt } \cos \theta$ and $y = \text{Vtsin } \theta - 5\text{t}^2$.

- (i) Find V and θ 2
- (ii) Find the time taken for the projectile to attain its maximum height. 1
- (iii) Find the range of the projectile.
- (b) The points $P(2ap, ap^2)$ and $Q(aq, aq^2)$ lie on the parabola $x^2 = 4ay$.
 - (i) Show that the equation of the chord PQ is (p+q)x 2y 2apq = 0
 - (ii) Show that the gradient of the tangent at P is p. 2
 - (iii) Prove that if the tangent at P is parallel to the normal at Q then PQ passes through the focus S
- (c) A particle moves in a straight line so that its acceleration is given by a = x-2, where x is its displacement from the origin.

 Initially, the particle is at the origin and has velocity v = 2
 - (i) Find the initial acceleration.
 - (ii) Show that $v^2 = (x-2)^2$
 - (iv) Find x as a function of t.

--End of Exam--

(3)
$$\beta$$
 $\frac{3}{2} = \frac{\pi}{2}, \frac{3\pi}{2\pi}, \frac{5\pi}{2\pi}, \dots$

(4)
$$B = a \cos^2 \delta x - \sin^2 \delta x$$

 $= a \cos^2 \delta x - (1 - a \cos^2 \delta x)$
 $= 2a \cos^2 \delta x - 1$
 $\frac{a \cos^2 \delta x - 1}{a \cos^2 \delta x}$

(6) C
$$\frac{1}{2}V^{2} = \Im 2 - \delta_{x}^{2}$$

$$\stackrel{\sim}{\chi} = -16x$$

$$h^{2} = 16$$

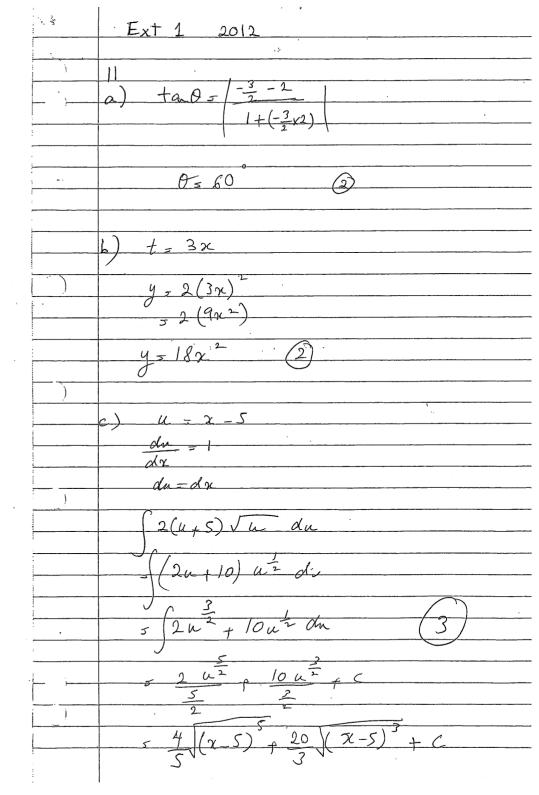
$$h = 4$$

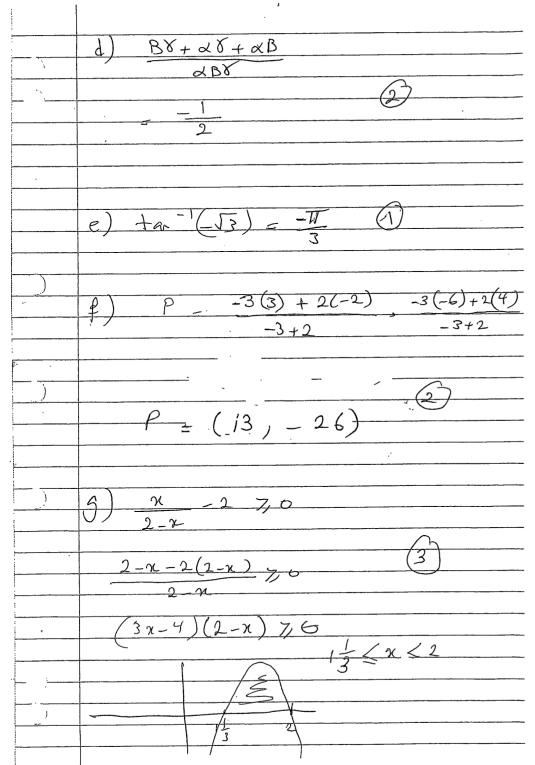
$$\stackrel{\sim}{T} = 2\pi$$

$$\stackrel{\leftarrow}{T}$$

(9) A
$$x = \frac{5}{2y-6}$$
 $x+2 = \frac{5}{2y-6}$
 $2y-6 = \frac{5}{2x+2}$
 $2y = \frac{5}{2x+2} + 6$
 $y = \frac{5}{2x+4} + 3$

(10) A $y = 6x = 2x$
 $y = 6x = 2x$
 $y = 6x = 2x$





Question 12.

I, Prove true when
$$n=3$$

LHS = 5

RHS = 20×3 -
= 59

= 125

LHS > RHS

LHS > RHS

II, Prove true for
$$n \ge k+1$$
.

RTP $5 > 20(k+1) - 1$.

1.e. Prove LHS-RHS>0

LHS-RHS =
$$5^{kH}$$
 - 20 (k+1) H

= 5^k . 5 - 20k-20+1

> 5 (20k-1) - 20k - 19

= $100k - 5$ - $20k - 19$

= $80k - 24$

>0 as when $k \ge 3$, $80k - 24 \ne 216$

IN Blah.

b) 1)
$$P(\text{docs not rain for a week}) = (\frac{1}{3})$$

$$= \frac{1}{2187}$$

ii)
$$P(sM) + P(MT) + P(TM) + P(WT) + P(TF) + P(FS)$$

$$= i \left(\frac{2}{3}\right)^2 \times \left(\frac{1}{3}\right)^5 \times 6$$

$$= \frac{8}{729} - \frac{8}{729}$$

C)
$$u = \sin \alpha$$

when $\alpha = \frac{1}{2}$
 $du = \cos \alpha$
 $du = \cos \alpha d\alpha$

when $\alpha = 0$, $u = \sin \alpha$
 $du = \cos \alpha d\alpha$

$$T = \int_{0}^{1} u^{2} du$$

$$= \int_{0}^{1} u^{3} du$$

BOCB 15 isoscelts

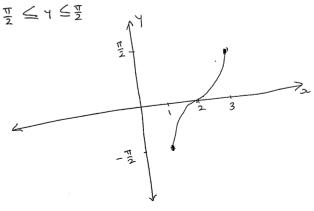
$$L = 40^{\circ} + 40^{\circ}$$

$$= 80^{\circ}$$

$$D: -1 \le \infty -2 \le 1$$

$$1 \le \infty \le 3$$

$$R: -\frac{\pi}{2} \leq \gamma \leq \frac{\pi}{2}$$



$$f) \quad f(\infty) = \sin \alpha - \frac{\alpha}{2}$$

$$f(2) = \sin(2)^{-\frac{2}{2}}$$

$$f'(2) = cos(2) - \frac{1}{2}$$
= -0.91615 --

$$x^5 = x' - \frac{\xi_1(x')}{\xi(x')}$$

$$=2-\frac{f(2)}{f'(2)}$$

$$= 2 - \frac{0.00907}{0.91615}$$

(a)
$$\int_{0}^{2} \frac{dx}{4x^{2} + 20} = \frac{1}{4} \int_{0}^{2} \frac{dx}{x^{2} + 5}$$

$$= \frac{1}{4\sqrt{5}} \left[\frac{1}{4} - \frac{x}{\sqrt{5}} \right]_{0}^{2}$$

$$= \frac{1}{4\sqrt{5}} \left[\frac{1}{4} - \frac{x}{\sqrt{5}} \right]_{0}^{2}$$

$$= \frac{1}{4\sqrt{5}} \left[\frac{1}{4} - \frac{x}{\sqrt{5}} \right]_{0}^{2}$$

(b) (i) LHS =
$$\frac{dT}{dt}$$
 $T = 20 + Ae^{-kt}$
= $-kAe^{-kt}$
= $-k(20 + Ae^{-kt} - 20)$
= $-k(T - 20)$
: LHS = RHS : $T = 20 + Ae^{-kt}$ is a soln.
of the equation

(ii) When
$$t=0$$
, $T=100$ when $t=15$, $T=70$

$$100 = 20 + A \Rightarrow A = 80$$

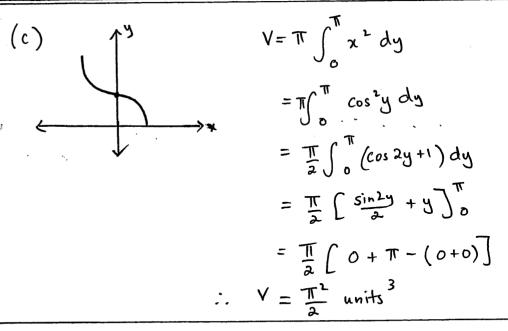
$$70 = 20 + 80 e^{-15k}$$

$$e^{-15k} = \frac{5}{8} \Rightarrow k = -\frac{1}{15} \ln \left(\frac{5}{8}\right) = 0.031$$

(iii)
$$25 = 20 + 80e^{-0.031t}$$

$$e^{-0.031t} = \frac{5}{80} \implies t = \frac{1}{6.031} \ln \left(\frac{5}{80} \right)$$

$$\therefore t \stackrel{?}{=} 88.5 \text{ minutes}$$



(d) (i)
$$P(x) = x^4 + 5x^3 + 4x^2 - 8x - 8$$

 $P(-1) = 1 - 5 + 4 + 8 - 8$
 $= 0$... $(x+1)$ is a factor
$$P(-2) = 16 - 40 + 16 + 16 - 8$$

$$= 0$$
 ... $(x+2)$ is a factor
Hence $(x+1)(x+2)$ is a factor

(ii)
$$(x^2 + 3x + 2) Q(x) = x^4 + 5x^3 + 4x^2 - 8x - 8$$

By inspection $Q(x) = x^2 + 2x - 4$

$$\frac{\sin \theta}{\cos \theta} = 2\sin \theta \cos \theta$$

$$\sin \theta = 0$$
 or $\cos \theta = \frac{1}{\sqrt{2}}$ $\frac{\frac{1}{\sqrt{2}}}{\sqrt{1}}$ $\frac{\frac{1}{\sqrt{2}}}{\sqrt{1}}$ $\frac{1}{\sqrt{2}}$

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Question 14
                             y=Vtsinθ-5t²
a) x = Vt cos 0
i) When x = 20,
                            4 = 5 Vsin 0 - 125
   20 = 5 V cos θ
   \frac{4 - V \cos \theta}{V = \frac{4}{\cos \theta}}
                     129 = V sinθ (2)
                                  iii) Time of flight = 2 x 2.58
  Sub (1) into 2
                                  Range = 26.1 x 5.16 x cos 81°11'
    129 = tan 0
     \theta = \tan\left(\frac{129}{20}\right)
         = 26.1 ms-1
 ii) Max height when y'=0
     y' = Vsin 8 - 10t
  V stind = 10 t
         = 2.58 s.
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```
b) P(2apap2) Q(2aq, aq2)
i) M = \frac{ap - aq}{2ap - 2aq}
       = a(p+q)(p-q)
2a(p-q)
        = p+9/
Equation of PQ:
    y-ap2 = p+9 (n-2ap)
   2y - 2ap^2 = (p+q)x - 2ap^2 - 2apq^2
  (p+q) x - 2y - 2apq = 0
   \chi^2 = 4ay
                         iii) If tangent at P is parallel to
                            normal at Q then gradient of
                            normal at Q is p and gradient of tangent at Q is -1.
    when n= 2ap
                            Substituting into PQ:
     \frac{dy}{dn} = \frac{2ap}{2a}
                           (p+q)x-2y+2a=0
                        when n=0
                                  -2y + 2a = 0
                         -: PQ passes through (0,a)
```

i) $\alpha = \pi - \lambda$ when $t = 0$, $x = 0$ $\alpha = -\lambda$ ii) $\alpha = \frac{d}{d\pi} \left(\frac{1}{2} v^2 \right)$ $\frac{d}{d\pi} \left(\frac{1}{2} v^2 \right) = x - \lambda$ $\frac{1}{2} v^2 = \int x - \lambda dx$ $v^2 = 2 \int x - \lambda dx$ $v^2 = 2 \int x - \lambda dx$ when $x = 0$, $y = \lambda$ $4 = 4 + C$ $C = 0$ $v^2 = (x - \lambda)^2$ iii) when $x = 0$ $y = \lambda$ $v = -(x - \lambda)^2$ $v = -(x - \lambda)^2$ $v = -(x - \lambda)$ $v =$	c)		
when $t=0$, $x=0$ $\therefore a=-\lambda$ ii) $a = \frac{d}{dx}(\frac{1}{2}v^2)$ $\frac{d}{dx}(\frac{1}{2}v^2) = x-\lambda$ $\frac{1}{2}v^2 = \int x-2 dx$ $v^2 = 2\int x-2 dx$ $= \chi(x-2) + C$ χ When $x=0$, $y=\lambda$ $4 = 4 + C$ $C = 0$ $\therefore v^2 = (x-2)^2$ iii) when $x=0$ $y=\lambda$ $t=-\ln(2-x) + C$ $v = -(x-2)$ when $t=0$, $x=0$ $v = \lambda - x$ $v = \lambda - x$ $dx = \lambda + x = -\ln(2-x) + \ln \lambda$.>	
ii) $a = \frac{d}{dx} \left(\frac{1}{2} v^2 \right)$ $\frac{d}{dx} \left(\frac{1}{2} v^2 \right) = x - 2$ $\frac{1}{2} v^2 = \begin{cases} x - 2 & dx \\ v^2 = 2 \end{cases} x - 2 & dx \end{cases}$ $= \chi \left(x - 2 \right) + C$ When $x = 0$, $y = 2$ $4 = 4 + C$ $C = 0$ $\therefore v^2 = (x - 2)^2$ iii) when $x = 0$, $y = 2$, $t = -\ln(2 - x) + C$ $\therefore v = -(x - 2)$ when $t = 0$, $t = 0$ $v = 2 - x$ $0 = -\ln 2 + C$ $\frac{dx}{dt} = 2 - x$ $C = \ln 2$			
ii) $a = \frac{d}{dx} \left(\frac{1}{2}v^{2}\right)$ $\frac{d}{dx} \left(\frac{1}{2}v^{2}\right) = x - \lambda$ $\frac{1}{2}v^{2} = \int x - 2 dx$ $v^{2} = 2 \int x - 2 dx$ $v^{2} = 2 \int x - 2 dx$ $when x = 0, y = \lambda 4 = 4 + C C = 0 v^{2} = (n - 2)^{2} iii) when x = 0, y = \lambda v = -(x - 2) v = 2 - x v = -(x - 2) v = 2 - x dx = 3 - x d$	_		
$\frac{d}{dx}\left(\frac{1}{2}v^{2}\right) = x - 2$ $\frac{1}{2}v^{2} = \int x - 2 dx$ $v^{2} = 2\int x - 2 dx$ $= \chi(n-2) + C$ χ When $x = 0$, $v = 2$ $4 = 4 + C$ $C = 0$ $x^{2} = (n-2)^{2}$ $v^{2} = (n-2)^{2}$ $v^{3} = (n-2)^{2}$ $v = -(n-2)$ $v = 2 - x$ $v = -(n-2)$ $v = 2 - x$ $0 = -\ln x + C$ dx dx dx dx dx dx dx dx	: a = -2	·	-
$\frac{d}{dx}\left(\frac{1}{2}v^{2}\right) = x - 2$ $\frac{1}{2}v^{2} = \int x - 2 dx$ $v^{2} = 2\int x - 2 dx$ $= \chi(n-2) + C$ χ When $x = 0$, $v = 2$ $4 = 4 + C$ $C = 0$ $x^{2} = (n-2)^{2}$ $v^{2} = (n-2)^{2}$ $v^{3} = (n-2)^{2}$ $v = -(n-2)$ $v = 2 - x$ $v = -(n-2)$ $v = 2 - x$ $0 = -\ln x + C$ dx dx dx dx dx dx dx dx	$d(1)^2$		-
$\frac{1}{2}v^{2} = \int n-2 dx$ $v^{2} = 2 \int x-2 dn$ $= \chi(n-2) + C$ χ When $n=0$, $y=2$ $4 = 4 + C$ $C = 0$ $x^{2} = (n-2)^{2}$ $y^{2} = (n-2)^{2}$ $y^{2} = (n-2)^{2}$ $y^{3} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{3} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{3} = (n-2) + C$ $y^{4} = (n-2) + $	$\frac{11}{2}$ $\frac{\alpha}{2}$ $\frac{1}{2}$		
$\frac{1}{2}v^{2} = \int n-2 dx$ $v^{2} = 2 \int x-2 dn$ $= \chi(n-2) + C$ χ When $n=0$, $y=2$ $4 = 4 + C$ $C = 0$ $x^{2} = (n-2)^{2}$ $y^{2} = (n-2)^{2}$ $y^{2} = (n-2)^{2}$ $y^{3} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{3} = (n-2) + C$ $y^{2} = (n-2) + C$ $y^{3} = (n-2) + C$ $y^{4} = (n-2) + $	$\frac{d}{d}\left(\frac{1}{2}\sqrt{2}\right) = \chi - 2$		
$v^{2} = 2 \int x - 2 dx$ $= \chi(x-2) + C$ χ When $x = 0$, $y = 2$ $4 = 4 + C$ $C = 0$ $x^{2} = (x-2)^{2}$ $y^{2} = (x-2)^{2}$ iii) when $x = 0$ $y = 2$ $t = -\ln(2-x) + C$ $y = -(x-2)$ when $t = 0$, $t = 0$ $y = 2 - x$ $0 = -\ln 2 + C$ $dx = 2 - x$ $dx = - \ln(2-x) + \ln 2$			
$= \chi(n-2) + C$ $= \chi(n-2) + C$ $= \chi(n-2) + C$ $= \chi$ When $x = 0$, $y = 2$ $= (n-2)^{2}$ $\therefore y^{2} = (n-2)^{2}$ $\therefore y^{2} = (n-2)^{2}$ $\therefore y^{2} = (n-2) + C$ $\therefore y = -(n-2) \text{when } t = 0, n = 0$ $y = 2 - \chi 0 = -\ln 2 + C$ $\frac{dn}{dt} = 2 - \chi C = \ln 2$ $\frac{dn}{dt} = 2 - \chi C = \ln 2$	$\frac{1}{2}v^2 = \left(n-2\right) dx$		
When $x=0$, $y=2$ 4 = 4 + C C = 0 $v^2 = (n-2)^2$ iii) when $x = 0$ $v = 2$ $t = -\ln(2-x) + C$ v = -(n-2) when $t = 0$, $v = 0v = 2-x 0 = -\ln 2 + Cdn = 2-x C = \ln 2dt = dt t = -\ln(2-x) + \ln 2$	$y^2 = 2 x-2 dr$		
When $x=0$, $y=2$ 4 = 4 + C C = 0 $v^2 = (n-2)^2$ iii) when $x = 0$ $v = 2$ $t = -\ln(2-x) + C$ v = -(n-2) when $t = 0$, $v = 0v = 2-x 0 = -\ln 2 + Cdn = 2-x C = \ln 2dt = dt t = -\ln(2-x) + \ln 2$	$= \sqrt{(x-2)}$	· · · · · · · · · · · · · · · · · · ·	
$4 = 4 + C$ $C = 0$ $\therefore v^{2} = (n-2)^{2}$ $\vdots v^{2} = (n-2)^{2}$ $\vdots v = -(n-2) \text{when } t = 0, n = 0$ $v = 2 - x 0 = -\ln x + C$ $\frac{dn}{dt} = 2 - x C = \ln 2$ $\frac{dn}{dt} = -\ln (2 - x) + \ln 2$	× ×	FC	-
$4 = 4 + C$ $C = 0$ $\therefore v^{2} = (n-2)^{2}$ $\vdots v^{2} = (n-2)^{2}$ $\vdots v = -(n-2) \text{when } t = 0, n = 0$ $v = 2 - x 0 = -\ln x + C$ $\frac{dn}{dt} = 2 - x C = \ln 2$ $\frac{dn}{dt} = -\ln (2 - x) + \ln 2$	When n=0, v=2	1.	
iii) when $x = 0$ $y = 2$ $t = -\ln(2-x) + C$ $\therefore y = -(x-2)$ when $t = 0$, $x = 0$ $y = 2-x$ $0 = -\ln 2 + C$ $\frac{dx}{dt} = 2-x$ $C = \ln 2$ $\frac{dx}{dt} = -\ln(2-x) + \ln 2$	C = 0		
$V = -(n-2) \text{when } t = 0, n = 0$ $V = 2 - x 0 = -\ln 2 + C$ $\frac{dn}{dt} = 2 - x C = \ln 2$ $-1 - dn = dt t = -\ln(2 - x) + \ln 2$	$\therefore V^2 = (\chi - 2)$		
$V = -(n-2) \text{when } t = 0, n = 0$ $V = 2 - x 0 = -\ln 2 + C$ $\frac{dn}{dt} = 2 - x C = \ln 2$ $-1 - dn = dt t = -\ln(2 - x) + \ln 2$	iii) when x = D v = 2	$t = -\ln(2-x) + C$	
$V = 2-x$ $D = -\ln 2 + C$ $dn = 2-x$ $C = \ln 2$ $-1 - dn = dt$ $t = -\ln(2-x) + \ln 2$			
$\frac{dt}{dt} = \frac{1}{2\pi t}$ $\frac{1}{2\pi t} = \frac{1}{2\pi t}$	V = 2-x	0 = - ln 2 + C	
$\frac{1}{1-dn} = dt$ $t = -\ln(2-x) + \ln 2$	dn = 2-x	C = 1n2	_
$\frac{1}{2-x} dn = dt \qquad t = -\ln(2-x) + \ln x$ $\ln 2 - t = \ln(2-x)$ $\pi = 2 - e^{\ln 2 - t}$ $= 2 - 2e^{-t}$		1 (0 0) 1 2	_
	$\frac{1}{2-n}$ dn = dt	$t = -\ln(2-\kappa) + \ln \kappa$	_
$= 2 - 2e^{-t}$		$\frac{\ln \lambda - t}{\lambda} = \frac{\ln \lambda - t}{\ln \lambda - t}$	_
AL PL.	· · ·	$= 2 - 2e^{-t}$	